



# Readings

- Reach chapter 2 of Buttazzo (2011)<sup>1</sup>
- Topics
  - Task schedule
  - Task preemption
  - Task timing
  - Metrics of scheduling algorithms



<sup>1</sup> Readings are based on Buttazzo, G. C. (2011). Hard Real-Time Computing Systems: Predictable Scheduling Algorithms and Applications (Real-Time Systems Series, 24) (3rd edition). Springer.

# Schedule

Given a **set of tasks**  $J = J_1, J_2, \dots, J_n$

- A **schedule** is an assignment of tasks to the processor, such that each task is executed until completion.
- A schedule can be defined as an **integer step function** (Equation (1))

$$\sigma : R \rightarrow N \quad (1)$$

where  $\sigma(t)$  denotes the task which is executed at time  $t$ . If  $\sigma(t) = 0$ , then the processor is called idle

- If  $\sigma(t)$  changes its value at some time, then the processor performs a **context switch**.
- Each interval, in which  $\sigma(t)$  is constant is called a **time slice**.
- A **preemptive schedule** is a schedule in which the running task can be arbitrarily suspended at any time, to assign the CPU to another task according to a predefined scheduling policy.

# Example—Task scheduling

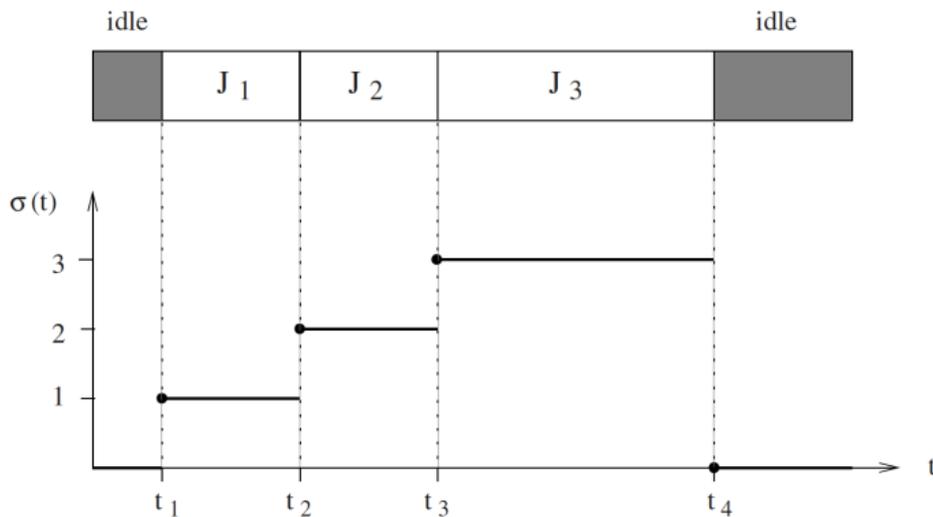


FIG 1. Schedule obtained by executing three tasks  $J_1$ ,  $J_2$ , and  $J_3$

- context switch at times  $t_1$ ,  $t_2$ ,  $t_3$ ,  $t_4$
- time slice—intervals  $[t_i, t_{(i+1)})$  in which  $\sigma(t)$  is constant

# Preemption

Preemption is important for three reasons:

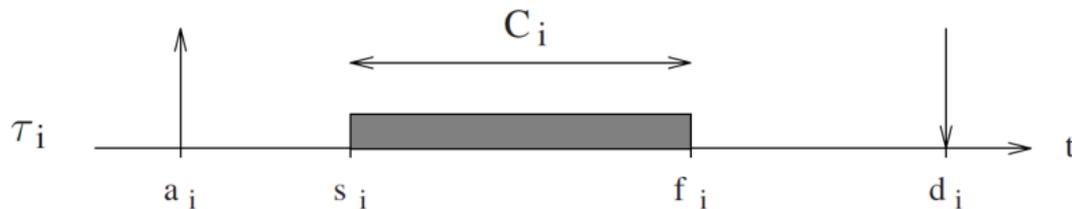
- 1 Tasks performing exception handling may need to preempt existing tasks so that responses to exceptions may be issued in a timely fashion.
- 2 When tasks have different levels of criticality (expressing task importance), preemption permits executing the most critical tasks, as soon as they arrive.
- 3 Preemptive scheduling typically allows higher efficiency, in the sense that it allows executing a real-time task sets with higher processor utilization.

Disadvantages:

- Preemption destroys program locality and introduces a runtime overhead
- This overhead increase the execution time of tasks.

# Schedule and Timing

A real-time task  $\tau_i$  can be characterized by the following parameters:



**FIG 2.** Typical parameters of a real-time task

- **feasible schedule**—if all task can be completed according to a set of specified constraints. Examples of constraints include:
  - Timing constraints—activation, period, deadline, jitter.
  - Precedence—order of execution between tasks.
  - Resources—synchronization for mutual exclusion.
- **schedulaable tasks**—If there exists at least one algorithm that can produce a feasible schedule.

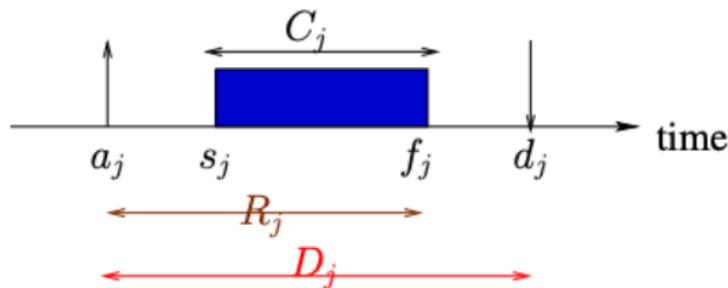
# Schedule and Timing

- **arrival time**  $a_i$  or **release time**  $r_i$  is the time at which a task becomes ready for execution
- **computation time**  $C_i$  is the time necessary to the processor for executing the task without interruption.
- **relative deadline**  $D_i$  is the time length between the arrival time and the absolute deadline.
- **absolute deadline**  $d_i$  is the time at which a task should be completed. Note that from the above definitions, we have the relation in **Equation** (2)

$$d_i \geq r_i + C_i \quad (2)$$

# Schedule and Timing

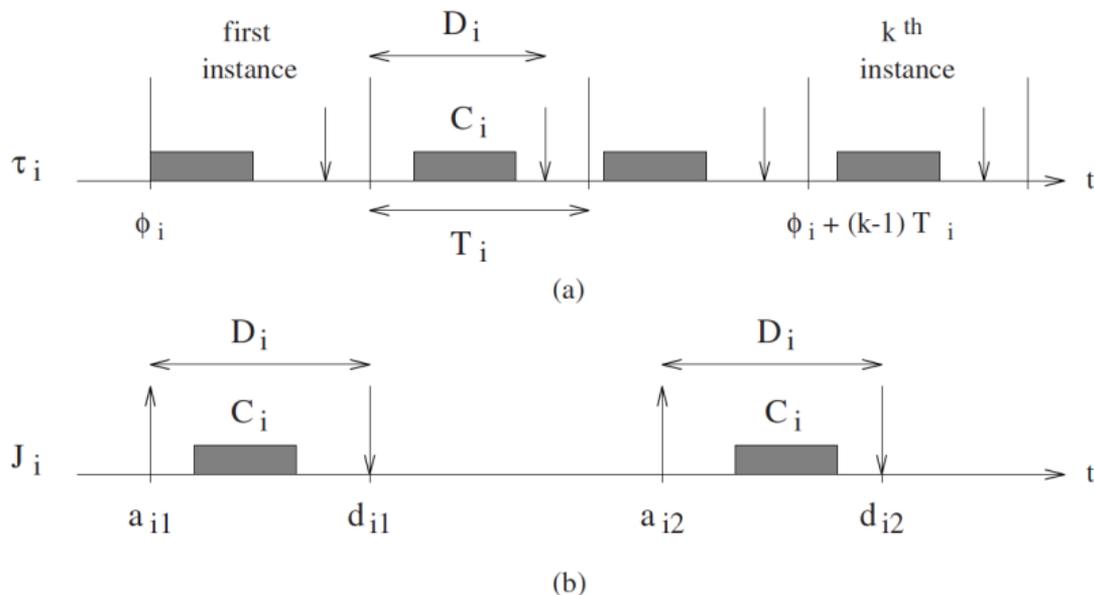
- **start time**  $s_j$  is the time at which a task starts its execution.
- **finishing time**  $f_j$  is the time at which a task finishes its execution.
- **response time**  $R_j$  is the time length at which the job finishes its execution after its arrival, which is  $f_j - a_j$



- **lateness**  $L_j = f_j - d_j$  represents the delay of a task completion with respect to its deadline. If a task completes before the deadline, its lateness is negative.
- **tardiness** or **exceeding time**  $E = \max(0, L_j)$  is the time a task stays active after its deadline.
- **laxity** or **slack time**  $X_j = d_j - a_j - C_j$  is the maximum time a task can be delayed on its activation to complete within its deadline.

# Schedule and Timing

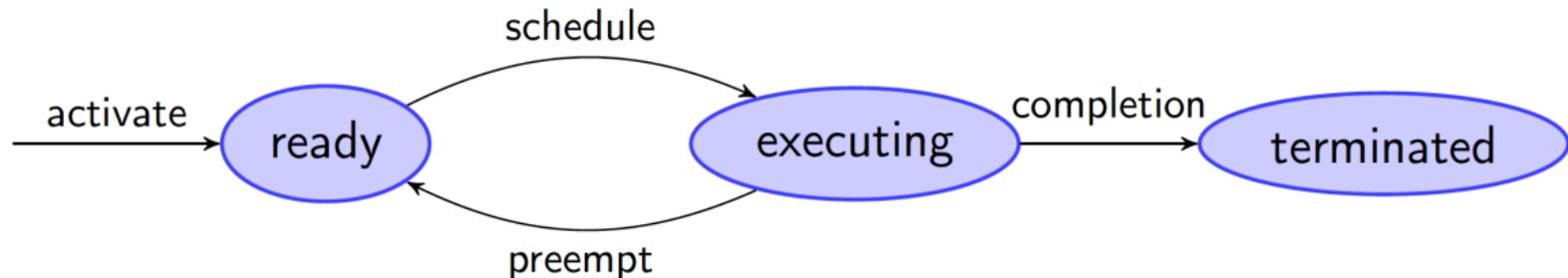
**periodic task**  $\tau_i$  —infinite sequence of identical activities, called **instances or jobs**, that are regularly activated at a constant rate with **period**  $T_i$ . The activation time of the first instance is called **phase**  $\phi$



**FIG 3.** Sequence of instances for a periodic task (a) and an aperiodic job (b)

# Scheduling Algorithm

**scheduling algorithm**—determines the order that jobs execute on the processor



- **preemptive algorithms**—the running task can be interrupted at any time to assign the processor to another active task, according to a predefined scheduling policy.
- **non preemptive algorithm**—a task, once started, is executed by the processor until completion.
- **static algorithms** are those in which scheduling decisions are based on fixed parameters, assigned to tasks before their activation.
- **dynamic algorithms** are those in which scheduling decisions are based on dynamic parameters that may change during system execution.

# Metrics of scheduling algorithms

- Average response time,  $\bar{t}_r$  (Equation (3))

$$\bar{t}_r = \frac{1}{n} \sum_{i=1}^n (f_i - a_i) \quad (3)$$

- Total completion time,  $t_c$  (Equation (4))

$$t_c = \max(f_i) - \min(a_i) \quad (4)$$

- Maximum lateness,  $L_{max}$  (Equation (5))

$$L_{max} = \max(f_i - d_i) \quad (5)$$

- Maximum number of late tasks

$$N_{late} = \sum_{i=1}^n \text{miss}(f_i), \quad (6)$$

with  $\text{miss}(f_i)$  defined as shown in Equation (7)

$$\text{miss}(f_i) = \begin{cases} 0, & \text{if } f_i \leq d_i. \\ 1 & \text{otherwise} \end{cases} \quad (7)$$

**The end**