

## BJT Circuits at DC

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### BJT DC analysis steps

Use the following steps when analyzing BJT circuits with DC voltages:

- 1 Assume that the transistor is operating in active mode.
- 2 Determine  $I_C$ ,  $I_B$ ,  $V_{CE}$  and  $V_{BE}$  using the active mode model.
- 3 Check for consistency of results with active-mode operation such as  $V_{CE} > V_{CEsat}$ .
- 4 If it is satisfied, the analysis is over.
- 5 If not, assume saturation mode and repeat the analysis like active mode.

This analysis is mainly used to identify the operating point.

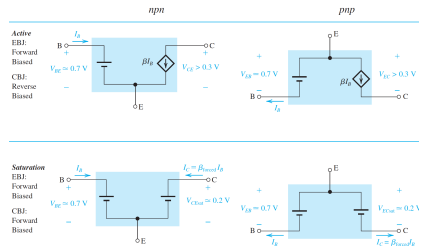


FIG 1. Simplified Models for the Operation of the BJT in DC Circuits

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### Example 1

In Fig. 2, if  $\beta = 100$  and  $V_{BE} = 0.7\text{ V}$ , which mode is the transistor operating in?

- Using Kirchhoff's Voltage Law (KVL) on the base-emitter loop (Equation (1))

$$4\text{ V} = V_{BE} + 3.3\text{ k}\Omega I_E \quad (1)$$

- Solving Equation (1) gives  $I_E = 1\text{ mA}$
- The base current  $I_B$  is calculated from its relationship to the emitter current

$$I_B = \frac{I_E}{\beta + 1} = 9.9\text{ }\mu\text{A} \quad (2)$$

- The collector current  $I_C$  is thus

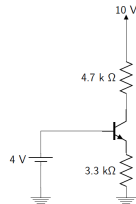


FIG 2. Example 1

## Example I

- To know the mode of operation of the transistors, we need to know  $V_{CE}$ .
- $V_{CE}$  is obtained by applying KVL on the CE loop as shown in Equation (4):

$$V_{CE} = 10V - 4.7k\Omega I_C - 3.3k\Omega I_E = 2.047 \quad (4)$$

- Since  $V_{CE} > V_{CEsat}$ , it is operating in active mode.

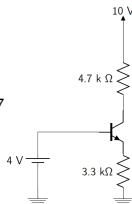


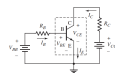
FIG 3. Example I

## NPN Common-Emitter circuit

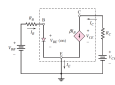
- We will assume that the BEJ is forward biased, so the voltage drop across that junction is the cut-in or turn-on voltage  $V_{BE(on)}$ .
- The base current is given in Equation (5)

$$I_B = \frac{V_{BB} - V_{BE(on)}}{R_B} \quad (5)$$

- Equation (5) implies that  $V_{BB} > V_{BE(on)}$ —which means that  $I_B > 0$ . Otherwise,  $V_{BB} < V_{BE(on)}$ .



(a) npn transistor common-emitter



(b) dc equivalent circuit.

FIG 4. Common emitter—Transistor equivalent circuit is shown within the dotted lines with piecewise linear transistor parameters.

## NPN Common-Emitter circuit

- The collector current is given Equation (6)

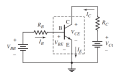
$$I_C = \beta I_B \quad (6)$$

- Kirchhoff's voltage law allows to compute  $V_{CC}$  and  $V_{CE}$

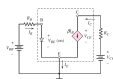
$$V_{CC} = I_C R_C + V_{CE} \quad (7)$$

$$V_{CE} = V_{CC} - I_C R_C \quad (8)$$

- Equation (8) implicitly assumes that  $V_{CE} > V_{CEsat}$ —which



(a) npn transistor common-emitter



(b) dc equivalent circuit.

FIG 5. Common emitter—Transistor equivalent circuit is shown within the dotted lines with piecewise linear transistor parameters.

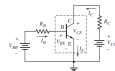
## NPN Common-Emitter circuit

- The power dissipated in the transistor is given by Equation (9)

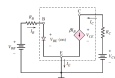
$$P_T = I_B V_{BE(on)} + I_C V_{CE} \quad (9)$$

- However, in most cases  $I_C \gg I_B$  and  $V_{CE} > V_{BE(on)}$ . Thus, Equation (9) can be simplified as shown in Equation (10)

$$P_T \approx I_C V_{CE} \quad (10)$$



(a) npn transistor common-emitter



(b) dc equivalent circuit.

FIG 6. Common emitter—Transistor equivalent circuit is shown within the dotted lines with piecewise linear transistor parameters.

## Example 11

Calculate the base, collector, emitter currents, the  $V_{CE}$  voltage and the transistor power dissipation for the common-emitter circuit shown in Fig. 7. Assume  $\beta = 200$  and  $V_{BE(on)} = 0.7 \text{ V}$

- The base current is found as

$$\begin{aligned} I_B &= \frac{V_{BB} - V_{BE(on)}}{R_B} \\ &= \frac{4 \text{ V} - 0.7 \text{ V}}{220 \text{ k}} \\ &= 15 \mu\text{A} \end{aligned} \quad (11)$$

- The collector current is

$$I_C = \beta I_B = 200 \times 15 \mu\text{A} = 3 \text{ mA} \quad (12)$$

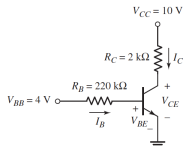


FIG 7. Example 2

- The emitter current is

$$I_E = (1 + \beta) I_B = 3.02 \text{ mA} \quad (13)$$

- The collector-emitter voltage is

$$V_{CE} = V_{CC} - I_C R_C = 4 \text{ V} \quad (14)$$

- The power dissipated is

$$\begin{aligned} P_T &= I_B V_{BE(on)} + I_C V_{CE} \\ &= 0.015 \times 0.7 + 3 \times 4 \\ &= 12 \text{ mW} \end{aligned} \quad (15)$$

- Since  $V_{BB} > V_{BE(on)}$  and

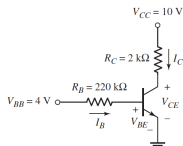


FIG 8. Example 2

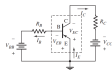
## PNP Common-Emitter circuit

- In Fig. 9, the emitter is at ground potential, which means that the polarities of the  $V_{BB}$  and  $V_{CC}$  power supplies must be reversed compared to those in the npn circuit.

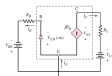
- The analysis proceeds exactly as before, and we can write:

$$I_B = \frac{V_{BB} - V_{EB(on)}}{R_B} \quad (16)$$

$$I_C = \beta I_B \quad (17)$$



(a) pnp transistor common-emitter



(b) dc equivalent circuit.

**FIG 9. Common emitter**—Transistor equivalent circuit is shown within the dotted lines with piecewise linear transistor parameters.

## Example 3

Find  $I_B$ ,  $I_C$ ,  $I_E$  and  $R_C$  such that  $V_{EC} = \frac{1}{2} V^+$  for the circuit given in Fig. 10. Assume  $\beta = 100$  and  $V_{EB(on)} = 0.6 \text{ V}$

$$I_C = \beta I_B = (100)(5 \mu\text{A}) \Rightarrow 0.5 \text{ mA}$$

and the emitter current is

$$I_E = (1 + \beta) I_B = (101)(5 \mu\text{A}) \Rightarrow 0.505 \text{ mA}$$

For a C-E voltage of  $V_{EC} = \frac{1}{2} V^+ = 2.5 \text{ V}$ ,  $R_C$  is

$$R_C = \frac{V^+ - V_{EC}}{I_C} = \frac{5 - 2.5}{0.5} = 5 \text{ k}\Omega$$

In this case,  $(V^+ - V_{BB}) > V_{EB(on)}$ . Also, because  $V_{EC} > V_{EB(on)}$ , the pnp bipolar transistor is biased in the forward-active mode.

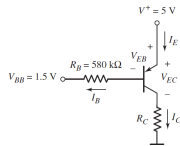


FIG 10. Example 3

**The end**